

Total No. of Questions – 24

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Total No. of Printed Pages - 3

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**Part - III**  
**MATHEMATICS, Paper – II (B)**  
**(English Version)**

**Time : 3 Hours]****[Max. Marks : 75****Note :** This question paper consists of **three** Sections A, B and C.**SECTION – A****10 × 2 = 20****I. Very Short Answer Type questions.**

- (i) Answer **all** questions.
- (ii) Each question carries **two** marks.

1. Find the equation of the circle passing through (3, 4) and having the centre at (–3, 4).
2. Find the centre and radius of the sphere  $x^2 + y^2 + z^2 - 2x + 4y - 6z - 2 = 0$ .
3. Find the value of 'K' if points (1, 2), (K, –1) are conjugate with respect to the parabola  $y^2 = 8x$ .
4. If the eccentricity of a hyperbola is  $5/4$ , then find the eccentricity of its conjugate hyperbola.
5. Find the  $n^{\text{th}}$  derivative of  $f(x) = \sin 7x \cos x \forall x \in \mathbb{R}$ .
6. Evaluate  $\int \left(x + \frac{1}{x}\right)^3 dx, x > 0$ .
7. Evaluate  $\int \frac{dx}{(x+1)(x+2)}$

8. Evaluate  $\int_2^3 \frac{2x}{1+x^2} dx$

9. Find the area of the region enclosed between  $y = x^3 + 3$ ,  $y = 0$ ,  $x = -1$ ,  $x = 2$ .

10. Form the differential equation corresponding to  $y = cx - 2c^2$ , where 'c' is a parameter.

## SECTION – B

5 × 4 = 20

### II. Short Answer Type questions.

(i) Answer any **five** questions.

(ii) Each question carries **four** marks.

11. Find the angle between the tangents drawn from (3, 2) to the circle

$$x^2 + y^2 - 6x + 4y - 2 = 0.$$

12. Find the condition for the line  $y = mx + c$  to be a tangent to the parabola

$$x^2 = 4ay.$$

13. Find the pole of the line  $21x - 16y - 12 = 0$  with respect to the ellipse  $3x^2 + 4y^2 = 12$ .

14. If PSQ is a chord passing through the focus S of a conic and  $l$  is semi latus rectum, show that  $\frac{1}{SP} + \frac{1}{SQ} = \frac{2}{l}$ .

15. Evaluate  $\int \frac{dx}{5 + 4 \cos x}$

16. Solve the differential equation  $(2x - y)dy = (2y - x)dx$

17. Solve the differential equation  $\frac{dy}{dx} + y \tan x = \sin x$ .

**III. Long Answer Type questions.**

- (i) Answer any **five** questions.  
(ii) Each question carries **seven** marks.

18. Find the equation of a circle which passes through (4, 1), (6, 5) and having the centre on  $4x + 3y - 24 = 0$ .
19. Find the coordinates of the limiting points of the coaxial system to which the circles  $x^2 + y^2 + 10x - 4y - 1 = 0$  and  $x^2 + y^2 + 5x + y + 4 = 0$  are two members.
20. Show that the poles of the tangents to the circle  $x^2 + y^2 = a^2 + b^2$  with respect to the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  lies on  $\frac{x^2}{a^4} + \frac{y^2}{b^4} = \frac{1}{a^2 + b^2}$ .
21. If  $y = \cos (m \log x)$ ,  $x > 0$ , then show that  $x^2 y_2 + x y_1 + m^2 y = 0$  and hence deduce that  $x^2 y_{n+2} + (2n + 1) x y_{n+1} + (m^2 + n^2) y_n = 0$ .
22. Obtain reduction formula for  $I_n = \int \tan^n x \, dx$ ,  $n$  being a positive integer,  $n \geq 2$  and deduce the value of  $\int \tan^6 x \, dx$ .
23. Show that  $\int_0^{\pi/2} \frac{x}{\sin x + \cos x} \, dx = \frac{\pi}{2\sqrt{2}} \log (\sqrt{2} + 1)$ .
24. Calculate the approximate value of  $\int_1^5 \frac{dx}{1+x}$ , by taking  $n = 4$  in the Simpson's rule.
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